

(Probabilistically Analysable Real-Time Systems)

Measurement-Based Probabilistic Timing Analysis in the presence of Buffer Resources

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13th WCET Workshop. July 9, 2013, Paris, France

This project and the research leading to these results has received funding from the European Community's Seventh Framework Programme [FP7/2007-2013] under grant agreement n° 249100.



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Motivation

- Critical Real-Time Embedded (CRTE) systems
 - > Used in Space, Aerospace, Transportation,... industries
 - ➢ More functional value → more computational power → more complex HW/SW
- Complex HW/SW affect time analysability
 - Makes it difficult for current timing analysis to compute trustworthy and tight WCET estimates
- Probabilistic Timing Analysis (PTA)
 - Not as mature as more conventional timing analysis techniques
 - Aims at enabling/simplifying the analysis of complex processor architectures



Background: Execution history (EH)

- Current architectures use EH to boost average-case performance by speculating on the future
 - > E.g.: temporal and spatial locality for caches
- Static timing analysis requires EH information
 - For example to determine whether a given memory access hits in cache STA needs to built
 - The full history of all access to the cache to keep the cache state current after every access → the more abstraction the more pessimism



Background: Controlling EH

- **There are increasing limitations** in acquiring EH info
 - Complex processor architectures (IP protected)
 - Incomplete and/or inaccurate documentation
 - Program information may be unknown at analysis time
- Reduction of available knowledge about HW/SW → pessimistic assumptions →

degradation of the tightness of the WCET

- Design HW and SW whose execution time behavior does not depend on EH
 - Without renouncing performance-accelerator HW features
 - Without affecting functional behavior
- Develop new timing analysis techniques to go with it



Background: PTA

- Approach:
 - Introduces randomisation into the timing behaviour of the hardware and software
 - The functional behaviour is left unchanged

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Provides new probabilistic timing analysis techniques

Want to know more?
 PROARTIS and PROXIMA





PRC

PROXIMA IP Project Consortium

Barcelona Supercomputer Center

Rapita Systems Ltd.

SYSGO

University of Padua

INRIA

Aeroflex Gaisler AB

AIRBUS Operations SAS

University of York

Astrium Satellites

IK4-IKERLAN

Infineon Technologies UK Ltd

Roles

•

- Academic research (BSC, UPD, INR, UoY)
- Tool chain providers at hardware (AG), software (SYS) and timing analysis (RPT) levels;
- Industrial exploitation via major EU companies and technology centres in the avionics, space, automotive, and railway sectors (AIF, AST, IFX, IKR)



ETP: Execution Time Profile

- In a PTA-conformant architecture:
 - The timing behaviour of instructions can represented with an Execution Time Profile (ETP).
 - ETP is the probability distribution function describing the different execution times that an instruction can take.

 $(\vec{l}, \vec{p}) = \{l_1, l_2, \dots, l_k\}\{p_1, p_2, \dots, p_k\}\sum_{i=1}^k p_i = 1$

- Do I have to change entirely my processor design?
 - ONLY certain hardware resources are randomised to achieve that behavior, e.g. cache [1] OR software-support for randomisation is used instead [2]



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Measurement-based PTA (MBPTA)

- Complete runs of the program are made on the time-randomised target platform
 - Measurements must capture outcome of events that make execution time vary
 - All potential execution times must have a probability of being exercised
 - > The ETP of processor instructions need <u>not</u> be known
 - Existence of ETP → guarantees ET act as a die with an arbitrarily large number of faces, each representing a distinct execution time
 - From this and sufficiently large number of i.i.d observations (in the order of hundreds) we can use EVT to derive pWCET estimations

L. Cucu, L. Santinelli, M. Houston, C. Lo, T. Vardanega, L. Kosmidis, J. Abella, E. Mezzetti, E. Quinones, F. J. Cazorla. **Measurement-Based Probabilistic Timing Analysis for Multi-path Programs** *ECRTS* 2012



Measurement-based PTA (MBPTA)

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 - Measurements must capture outcome of events that make execution time vary

All potential execution times must have a probability of being exercised 1,0E+00



pWCET

Simple Processor Resources

- The existence of ETP ensures i.i.d behavior
 - ETP is the implementation of a random variable
 - How is this obtained?
- *Jitter:*
 - Difference between the best & worst latency of any resource
 - > Due to the history of requests or the data cotained in request
- Jitterless resources
 - > No response time variation
- *Jittery resources*
 - Variable impact on the WCET whose significance depends
 - The program under study
 - The analysis method





Dealing with jittery resources (no timing anomalies)

- Force that the requests to the resources incur the worstcase latency.
 - Acceptable if the cumulative impact on the WCET is deemed low enough by the system designer
- Worst latency is not acceptable → randomise the timing behaviour of the resource (e.g. caches)



Resources \rightarrow instructions

• This simple resource classification does not cover more complex resource such as buffers

Instructions

- Access multiple resources that can be arranged in different manners, e.g. sequentially or in parallel.
- Under each arrangement, the ETP of those resources can be properly combined to derive the ETP of the instruction.

July 09, 2013

> Convolution

Buffers in MBPTA: Example

- Two stages (fetch and execute) that respectively access time randomised caches^{1,2}: IL1 and DL1.
 - Probability of hit for every access
- In between both stages there is a 2entry buffer



- > i1 may introduce delays on i2-i4 if it misses in DL1 (IL1 hit prob. Is 1.0)
- i2-i4 make no data cache access

| instruction | instruction | | L1 | DL1 | | | |
|-------------|-------------|-----------|------------|---------------------|------------------|--|--|
| id | type | hit prob. | miss prob. | hit prob. | miss prob. | | |
| il | ĹĎ | 1.0 | 0.0 | 0.9 | 0.1 | | |
| i2 | ADD | 0.7 | 0.3 | - 0 <u>-</u> | | | |
| i3 | ADD | 0.6 | 0.4 | - 19 - 5 | 5. : | | |
| i4 | ADD | 1.0 | 0.0 | - | - | | |

1 Leonidas Kosmidis, Jaume Abella, Eduardo Quinones and Francisco Cazorla. Cache Design for Probabilistic Real-Time Systems. DATE 2013

2 L. Kosmidis, C. Curtsinger, E. Quinones, J. Abella, E. Berger and Francisco Cazorla. Enabling Probabilistic Timing Analysis Through Compiler and Run-Time Support. DATE 2013

Chronograms: <DL1-i1, IL1-i2, IL1-i3>

| | <H,H,H> – P(HHH) = 0.378 | | | | | | | | | | | | |
|------------|--------------------------|---|---|---|---|---|---|---|---|----|----|----|----|
| | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 |
| i1 | F | b | Е | | | | | | | | | | |
| i 2 | | F | b | E | | | | | | | | | |
| i3 | | | F | b | E | | | | | | | | |
| i4 | | | | F | В | E | | | | | | | |
| | No buffer stalls | | | | | | | | | | | | |

<H,H,M> – P(HHM) = 0.252

| | | | , | ,- | - | - \ | | , | - | | - | | |
|----|---|---|---|----|-----|------|------|------|---|----|----|----|----|
| | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 |
| i1 | F | b | Ε | | | | | | | | | | |
| i2 | | F | b | E | | | | | | | | | |
| i3 | | | F | F | F | b | E | | | | | | |
| i4 | | | | | | F | b | Е | | | | | |
| | | | | 1 | Mal | huff | or o | tall | | | | | |

No buffer stalls

| | | | <h,< th=""><th>M,I</th><th>-<i< th=""><th>- P(</th><th>HM</th><th>H)</th><th>= 0</th><th>.162</th><th>2</th><th></th></i<></th></h,<> | M,I | - <i< th=""><th>- P(</th><th>HM</th><th>H)</th><th>= 0</th><th>.162</th><th>2</th><th></th></i<> | - P(| HM | H) | = 0 | .162 | 2 | |
|-----|---|---|---|-----|--|------|----|----|-----|------|---|------|
| - 1 | - | _ | _ | | _ | - | _ | _ | - | | | |

| | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 |
|------------|---|---|---|---|---|-----|---|------|---|----|----|----|----|
| i 1 | F | b | Ε | | | | | | | | | | |
| i 2 | | F | F | F | В | E | | | | | | | |
| i3 | | | | | F | b | Ε | | | | | | |
| i4 | | | | | | F | b | E | | | | | |
| | | | | | | 1 0 | ~ | . 11 | | | | | |

No buffer stalls

< M H H > - P(MHH) = 0.042

| 1 2 3 4 5 6 7 8 9 10 11 12 13 | | | | ~141 | ,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,, | .12 | - 1 (| TATT: | шj | - 0 | .042 | - | | |
|-------------------------------|------------|---|---|------|---|-----|-------|-------|----|-----|------|----|----|----|
| | | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 |
| il F b E E E E E E E E | i 1 | F | b | E | E | E | Е | E | E | Ε | Ε | | | |
| i2 F b b B b b b b b E | i2 | | F | b | b | В | b | b | b | b | b | Е | | |
| i3 F b B b b b b b E | i3 | | | F | b | В | b | b | b | b | b | b | E | |
| i4 F F F F F F b b E | i4 | | | | F | F | F | F | F | F | F | b | b | Е |

i4: 6 cycles of buffer stall

|--|

| | | | | | | | • | | | | | | |
|------------|---|---|---|------|---|---|------|----|---|-----|----|----|----|
| | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 |
| i 1 | F | b | E | E | E | E | E | E | E | E | | | |
| i2 | | F | F | F | В | b | b | b | b | b | E | | |
| i3 | | | | | F | b | b | b | b | b | b | E | |
| i4 | | | | | | F | F | F | F | F | b | b | Ε |
| | | - | | i. A | | | -f 1 | cr | | -11 | | - | |

i4: 4 cycles of buffer stall

<H,M,M>-P(HMM)=0.108

| | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 |
|----|---|---|---|---|-----|------|------|------|-----|----|----|----|----|
| i1 | F | b | Е | | | | | | | | | | |
| i2 | | F | F | F | В | E | | | | | | | |
| i3 | | | | | F | F | F | b | Е | | | | |
| i4 | | | | | | | | F | b | Ε | | | |
| | | | | | No. | huft | AT 0 | tall | e . | | | | |

No buffer stalls

<M,H,M>-P(MHM) = 0.0289 10 11 12 13 2 3 4 5 6 8 7 E Е F b Ε E E E Ε Е i1 i2 F в Ε b b b b b b b i3 F F F E b b b h b b i4 F F F Ε F F b b

i4: 4 cycles of buffer stall



Observation

- Given a set of fixed (or probabilistic¹) initial conditions
 - Each combination of prob. events (e.g. DL1 and IL1 accesses)
 one fully-deterministic behaviour of the buffer.
- Buffer introduces a different number of stall cycles for each combination of probabilistic events.
 - For a sequence of random events the behaviour of the buffer is fully deterministic
 - All data dependences, which are given by the sequence of instructions that are executed and their order.
- MBPTA works or a per-path basis → in each path the sequence of instructions executed is known and fixed across runs of the same path.
- Buffers do not introduce new probabilistic events! Increase the 'latency' under some prob. event outcome

1 Leonidas Kosmidis, Eduardo Quiñones, Jaume Abella, Tullio Vardanega and Francisco J. Cazorla. Achieving Timing Composability with Probabilistic Timing Analysis. ISORC 2013.







- (i) History dependence
 - Whether the jitter is produced solely by the event under consideration (no history dependence) or
 - The combination of previous events and the current one (history dependence);
 - History Dependent (HD) or not History Dependent (nHD)
- (ii) Type of jitter
 - > whether the jitter is deterministic (**DJ**)
 - probabilistic (PJ) or
 - simply propagated/transmitted regardless of its source (TJ)

• noHD + DJ

- Resource's latency does not depend on the sequence of requests it has received, but on the data of each request.
- > Some FP unit in is affected by the particular operands
 - We force it to experience worst latency
 - Worst-case mode [1].
- noHD + PJ
 - > We do not have any particular realistic example of this type
- noHD + TJ
 - In principle such a resource cannot exist because it does not produce any jitter by itself and cannot propagate any jitter if it is history independent

1 Marco Paolieri, Eduardo Quinones, Francisco J. Cazorla, Guillem Bernat and Mateo Valero. Hardware Support for WCET Analysis of Multicore Systems . ISCA 2009.



• HD + PJ

- > Time randomised cache
- The sequence of events between two consecutive accesses to the same data together with the initial cache state, determine the hit/miss probability of that access.
 - Time randomised caches have been shown to be analysable with MBPTA [1].
- HD + DJ
 - > Deterministic cache (e.g modulo+LRU)
 - > Events may experience different latencies depending on history
 - Not analysable by MBPTA unless the factors that influence jitter are fully under control

 Liliana Cucu-Grosjean, Luca Santinelli, Michael Houston, Code Lo, Tullio Vardanega, Leonidas Kosmidis, Jaume Abella, Enrico Mezzeti, Eduardo Quinones, Francisco J. Cazorla.
 Measurement-Based Probabilistic Timing Analysis for Multi-path Programs. ECRTS 2012.

• HD+ TJ

- > This is the case of a hardware buffer.
- An instruction may spend a different number of cycles in a buffer depending on previous events.
- Propagate deterministically the effect of the jitter induced by other resources.
 - If such jitter is probabilistic, then the stalls induced by buffers occur also with a given probability and so they are



July 09, 2013

Conclusions

Buffer resources

- > Do not create any jitter on their own
- > They propagate inbound jitter regardless of the nature of it.
- Do not introduce new probabilistic events! Increase the 'latency' of some prob. events
- > Do not break PTA requirements,
- Can be used in PTA-conforming processors with <u>no change</u>.
- Provide a comprehensive classification of hardware resources and how they can be considered in the context of PTA.





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