

# The Auspicious Couple: Symbolic Execution and WCET Analysis

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Motivation

Introduction

Symbolic  
Execution in  
r-TuBound

Symbolic  
Execution  
without Path  
Explosion

Conclusion

# WCET Analysis

## WCET Analysis

- ▶ mandatory for safety-critical real-time systems

## Computed WCET bounds

- ▶ must be **safe**
- ▶ shall be **tight**

## Problem

- ▶ precise knowledge about the program

# Symbolic Execution

## Symbolic Execution

- ▶ use **symbolic** instead of concrete data

## Control-flow split (branch)

- ▶ follow both paths
- ▶ assume respective condition

## Problem: path explosion

- ▶ unbounded loops
- ▶ number of conditionals

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# Our Remedy

Combine symbolic execution and WCET analysis as a remedy

**WCET analysis guides** symbolic execution

- ▶ select only WCET relevant parts

Symbolic execution **infers precise information**

- ▶ for relevant parts

**Partial** vs **full** symbolic coverage

- ▶ full symbolic coverage often infeasible in practice

**Partial** coverage often good enough to improve the WCET estimate

# r-TuBound

The  
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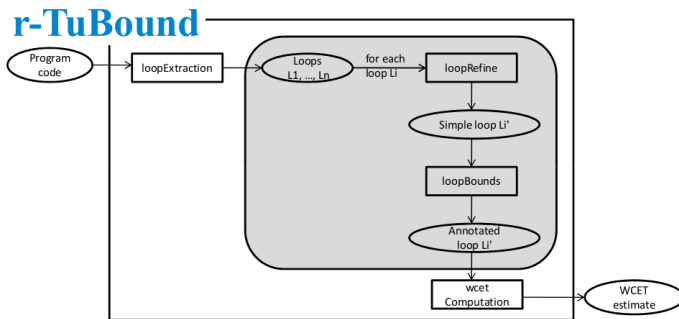
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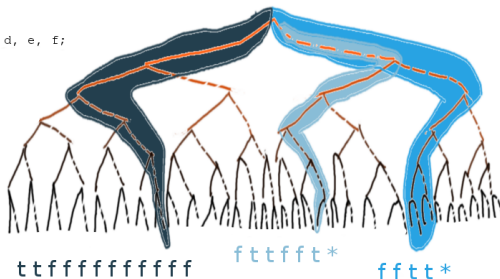
# Symbolic Execution: SmacC

## SmacC

- ▶ SMT representation of the program (BV, arrays)
- ▶ select paths via path-expressions

## Exact analysis

```
int main ()  
{  
  int cnt = 0;  
  int a, b, c, d, e, f;  
  
  if (a)  
    cnt++;  
  
  if (b)  
    cnt++;  
  
  if (c)  
    cnt++;  
  
  if (d)  
    cnt++;  
  
  if (e)  
    cnt++;  
  
  if (f)  
    cnt++;  
  
  return cnt;  
}
```



Full symbolic coverage requires execution of all paths!

# Symbolic Execution in r-TuBound

## 1) on selected program **fragments**

- ▶ check properties on conditional updates to the loopcounter
- ▶ if successful, loop bound computation safe

## 2) on single **loops**

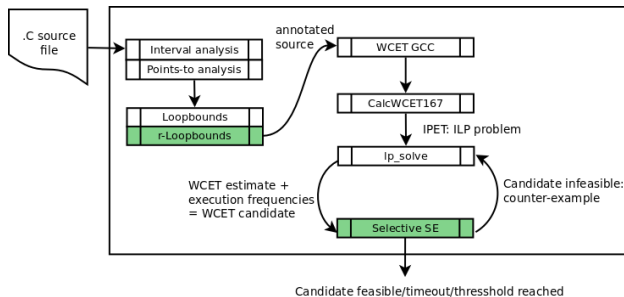
- ▶ only if all other techniques fail

## 3) on **single paths**

- ▶ as **post-process**, after initial WCET analysis
- ▶ symbolically **check feasibility of WCET path**

**= Selective Symbolic Execution**

# Architecture



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# Analyzing Program Fragments

Conditional update to loop counter  $i$  prevents bound calculation

```
int main (int flag) {  
    int i;  
    for (i = 0; i < 5; i++)  
        if (i == 4 && flag) {  
            i = 0;  
            flag = 0;  
        }  
}
```

## Success

- ▶ apply bound computation
- ▶ (combined minimal update)

## Fails for example

- ▶ verify that updates **strictly increase(decrease)**  $i$
- ▶ can check arbitrary expressions (in bitvectors/array theory)

# Loop Bounds via Symbolic Execution

(r-)loopbounds fails to compute a loop bound

only then

- ▶ apply exhaustive symbolic execution of the loop

The loop + required decls + additional analysis information

- ▶ = reduced program
- ▶ example: program = reduced program

Symbolically execute reduced program

- ▶ with initial bound 0
- ▶ increase bound while loop cond is SAT in last iteration

Example: loop bound 9

# Precise WCET Bounds

a.k.a **WCET Squeezing**

- ▶ post-processor for IPET based WCET analyzer
- ▶ allows to tighten WCET estimates
- ▶ ultimately prove WCET bounds precise

Is a combination of WCET analysis and symbolic execution

- ▶ **overcomes problems inherent in both approaches!**

# Problems of the Approaches

Symbolic Execution deficiency: **path explosion**  
(doesn't scale due to exponential number of paths)

IPET deficiency: considers **little** information about the program  
(flow-facts)

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# Some Remedy

**Combine IPET and Symbolic Execution for mutual benefit!**

extract path from ILP result and symbolically execute it

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# Some Remedy

## Combine **IPET** and **Symbolic Execution** for mutual benefit!

extract path from ILP result and symbolically execute it

Path explosion:

- ▶ less severe, initially **examine only one path**

Lack of information:

- ▶ rule out infeasible paths using **precise** symbolic execution
- ▶ by deriving new ILP constraints

Requires an initial WCET analysis

# Squeezing in a Nutshell

**in:** ILP problem (from IPET), **out** wcet bound

1. solve ILP problem
2. extract “**abstract**” WCET path candidates from ILP
3. compute “**concrete**” path(s) encoded by abstract path
4. **symbolically execute** concrete path(s)
5. use result of execution to **refine** ILP problem **or stop**:
  - 5.1 path feasible: done (path is indeed WCET path)
  - 5.2 infeasible: refine ILP, goto 2

On termination:

- ▶ **precise WCET bound** (wrt the HW-model)
- ▶ optional: timeout, threshold

# Expected Results

Refined WC path is feasible:

- ▶ real WCET-path, overestimation due to hardware modelling
- ▶ precise bound

Refined WC path is infeasible + TO:

- ▶ some improvement after a few iteration
- ▶ estimate tightened

ILP WC path is feasible:

- ▶ no gain in precision
- ▶ precise bound



# Example

Loop bound = 9

- ▶ analyze example with r-TuBound
- ▶ yields WCET estimate + ILP solution  
(computed from generated ILP problem)

ILP

- ▶ problem: constraints on execution frequencies
- ▶ solution: valid execution frequencies of blocks
- ▶ example: execution frequency of `then-block` = 9

The solution is **INFEASIBLE**

- ▶ no such concrete execution exists
- ▶ therefore, WCET bound is an over-estimation

## Example contd.

ILP solution “executes” then-block 9 times

Path-expression: `tttttttttt` (for the `if`-cond)

- ▶ i.e. iteration 0 to 9 execute then-branch
- ▶ i.e. **conditional evaluates to true 9 times**

```
int main (int flag) {
    int i;
    for (i = 0; i < 5; i++)
        if (i == 4 && flag) {
            i = 0;
            flag = 0;
        }
}
```

- ▶ path-expression can be constructed from ILP
- ▶ specifies a symbolic execution of the program

Result of symbolic execution defines further steps

- ▶ **feasible path**: terminate, bound precise
- ▶ **infeasible path**: derive ILP constraint to exclude the path, recompute WCET bound

# Example contd.

Squeezing the example:

- ▶ initially, 9 times `true-block`

Iteration 1:

- ▶ path infeasible, add constraint to exclude this path
- ▶ results in tighter solution

... Iteration 8 (terminating iteration):

- ▶ exact execution frequency inferred
- ▶ `true-block` once!

# Constraints

## Syntactic:

- ▶ comparable to a graph transformation
- ▶ introduces new ILP variables

## Semantic:

- ▶ constraint over combined execution frequency of involved conditions
- ▶ requires more symbolic executions

## Combination seems most effective

- ▶ peel a loop iteration (syntactic)
- ▶ constrain combined execution frequency up to peeled iteration

# Discussion

Squeezing can be stopped at any time (time-limit)

Squeezing can be run until a specified improvement is observed

Relies on **Partial symbolic coverage**

full symbolic coverage if all but one paths are infeasible

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Squeezing can be stopped at any time (time-limit)

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Relies on **Partial symbolic coverage**

full symbolic coverage if all but one paths are infeasible

All 3 presented approaches

- ▶ are effective
- ▶ require only partial symbolic coverage

# Further Applications

All 3 based on a similar symbolic execution infrastructure

- ▶ again, requiring **only partial symbolic coverage**

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**Precise execution frequencies for loops**

- ▶ iff symbolic execution is applied to find a loop bound

⇒ **cheap to track execution frequencies**



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## Precise execution frequencies for loops

- ▶ iff symbolic execution is applied to find a loop bound

⇒ **cheap to track execution frequencies**

## WCET path test-cases

- ▶ instantiate symbolic (input) variables (in SAT case)

⇒ use concrete values as **test input**

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## Precise execution frequencies for loops

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## WCET path test-cases

- ▶ instantiate symbolic (input) variables (in SAT case)

⇒ use concrete values as **test input**

## Mode-sensitive WCET analysis

- ▶ modify program after WCET analysis

⇒ squeezing to **automatically adapt IPET** constraints accordingly

# Conclusion

Symbolic execution is a powerful program analysis technique

- ▶ ... that “doesn’t scale”
- ▶ and therefore **shouldn’t rely on full symbolic coverage**

WCET analysis requires precise information about the program

- ▶ ... its result can serve as a **selection mechanism**
- ▶ to guide symbolic execution towards relevant program parts

**The combination of symbolic execution is promising:**

- ▶ WCET guidance is a **remedy to the path explosion** problem
- ▶ while symbolic execution helps **inferring tighter bounds**

⇒ 3 approaches successfully implemented in r-TuBound

⇒ 3 new approaches that can make use of the infrastructure

# Thanks for your Attention!

## Questions?

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# Examples - Binary Search

“Precise” analysis, e.g. array content

1) Mälardalen, `bs.c`, all data initialized

- ▶ from theoretic WC path of `bs` to **real WC execution path**

2) Mälardalen, `bs.c` modified, **some** data initialized

- ▶ from theoretic WC path of `bs` to a **better WC path**

3) Mälardalen, `bs.c` modified, **no** data initialized

- ▶ theoretic WC path of `bs` **is real WC path**

# Case 1 – Original Benchmark

```
1 int keys[15], vals[15];
2 int bs() {
3     int x = 8, fvalue = -1, mid, up = 14, low = 0;
4     keys = { ... }; // ALL initialized
5     vals = { ... }; // ALL initialized
6     while ( low <= up ) {
7         mid = (low + up) >> 1;
8         if ( keys[mid] == x ) {
9             up = low - 1;
10            fvalue = vals[mid];
11        } else if ( keys[mid] > x )
12            up = mid - 1;
13        else low = mid + 1;
14    }
15    return fvalue;
16 }
```

# Case 1 – Path Expression

by IPET: L1L1L1L1L1L1L1L1L1T

- ▶ L/T ... loop condition holds/does not hold
- ▶ 1, 2, 3 ... conditional blocks executed
- ▶ ? ... one of the conditional blocks executed

**infeasible!**

feasible execution by SE: **L2L3L2L1T**

## Case 2 – Modified Benchmark

```
...  
int bs() {  
    ...  
    keys = { ... }; // SOME initialized  
    vals = { ... }; // SOME initialized  
    ...  
}
```

PE by IPET: L1L1L1L1L1L1L1L1L1T **infeasible!**

feasible execution by SE: L2L3L?L?L?T, hence select

**L2L3L1L1L1T**



# Case 3 – Modified Benchmark

```
...  
int bs() {  
    ...  
    keys = { ... }; // ALL uninitialized  
    vals = { ... }; // ALL uninitialized  
    ...  
}
```

PE by IPET: **L1L1L1L1L1L1L1L1T** feasible by SE!

hence select **L1L1L1L1L1L1L1L1T**

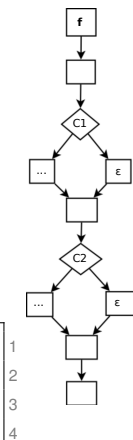
# Naive Refinement – Graph Level

## Split decision nodes

- ▶ double part of the CFG to rule out one path
- ▶ might blow up ILP problem

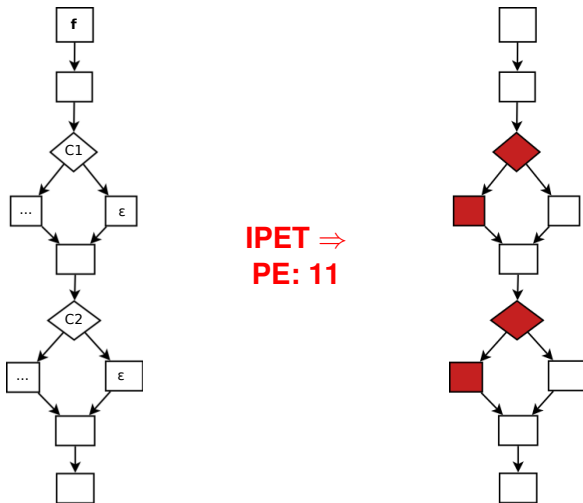
## Example 2

```
void f () {  
    if (C1) { ... }  
    if (C2) { ... }  
}
```



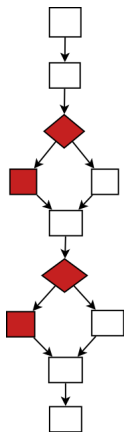
modes of operation: mutually exclusive execution parts

# Graph Refinement I: Extract WC Path

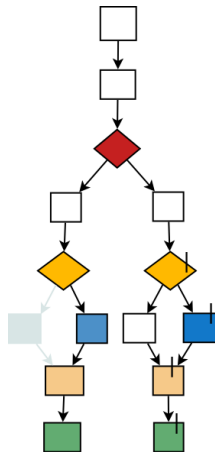


Construct **PE** from IPET solution

# Graph Refinement II: Split WC Path



SE  $\Rightarrow$   
infeasible



Symbolically execute PE, **split** if execution is **infeasible**.

# ILP Refinement: ILP Encoding

Step 1: as in graph approach (extract WC path)

Step 2: infeasible path  $\Rightarrow$  **ILP path constraint**

```
N = 1 // entry
b1 ≤ N
c1 ≤ b1
t1 + f1 ≤ c1
b2 ≤ c1
c2 ≤ b2
t2 + f2 ≤ c2
b3 ≤ c2
X ≤ b3
X ≤ 1 // exit
```

**restriction:**  
**!(t1 ∧ t2)**

```
N = 1
b1 ≤ N
c1 ≤ b1
t1 + f1 ≤ c1
b2 ≤ c1
c2 ≤ b2
t2 + f2 ≤ c2
b3 ≤ c2
X ≤ b3
X ≤ 1
t1 + t2 ≤ 1
```

Step 3: add constraint and restart ILP solver.

$\Rightarrow$  better WCET estimate.

# ILP Refinement: Loop Blocks

Alternative 1: peel loop, reduce frequency, add path constraint.

Alternative 2: path constraint including conditional block.

```
N = 1;
c1 = N;
t1 + f1 = c1;
loopHead = 1;
loopBody =
    loopHead *
    5;
loopBody = t2 +
    f2;
loopExit =
    loopHead;
X = loopExit;
```

**restriction:**  
**!(t1  $\wedge$  5t2)**

```
N <= 1;
c1 <= N;
t1 + f1 <= c1;
loopHead <= 1;
loopBody <=
    loopHead *
    5;
loopBody <= t2 +
    f2;
loopExit <=
    loopHead;
t1 + t2  $\leq$  5
X = loopExit;
```

Add constraint and restart ILP solver.

## **DdFR**: Demand-driven Feasibility Refinement to automatically

- ▶ refine WCET estimates on-demand, by
- ▶ selective symbolic execution and
- ▶ automatic construction of restrictive ILP clauses

that constrain the ILP search for a new WCET candidate.

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# Encoding of Counterexamples

A counterexample is:

- ▶ **infeasibility** of a WC path

Control-flow graph level:

- ▶ naive, inefficient
- ▶ program transformation

ILP level:

- ▶ more efficient
- ▶ force solver to generate different solution



# Further Benefits & Possibilities

Allows for and supports additional analyses

- ▶ before flow-fact computation (**whole program**)
- ▶ after WC path analysis (**path**)

Allows for combination with other approaches

- ▶ *criticality* – [Brandner/Hepp/Jordan, RTNS12]
- ▶ test-case generation – measurements on WC path
- ▶ concolic execution

# Current State

WC Path extraction: automatic

- ▶ modified CalcWCET167

Symbolic Execution: automatic

- ▶ preliminary, SmacC (C subset)
- ▶ PE translation needed, manual

Path generation / counterexample encoding: manual

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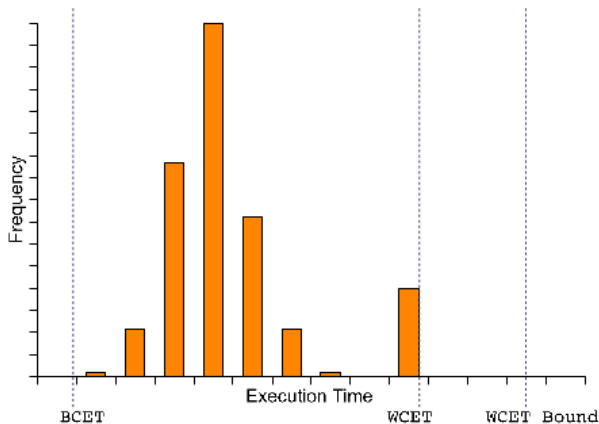
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# WCET Bound



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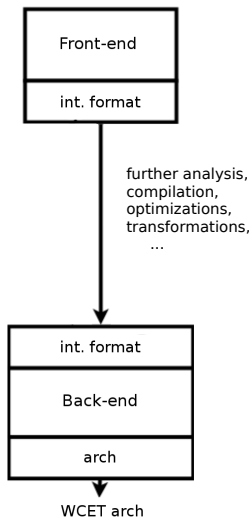
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# WCET Analysis Tool Chain



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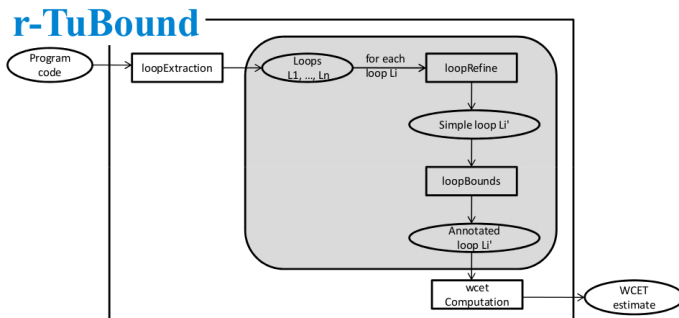
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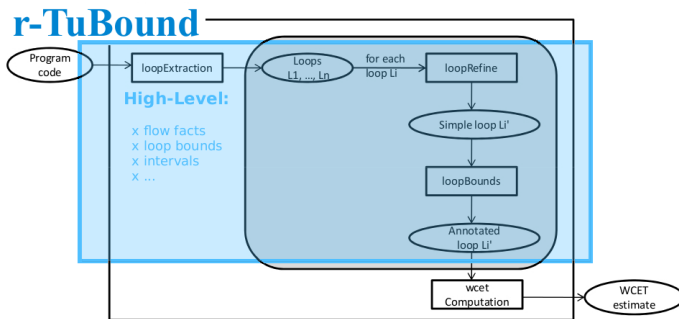
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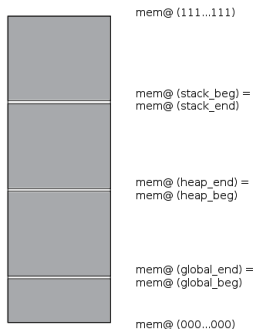
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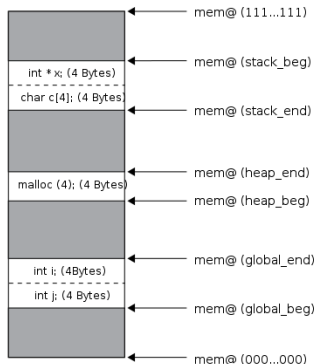
# Memory Model

- ▶ BTOR array/variables: memory of program / address mem
- ▶ special variables define valid memory

no variables declared



variables `x`, `c`, `i`, `j`, `malloc (4)`



# Assertion Check

```
void main () { int i; assert (i); }
```

BTOR variables:

```
{mem, global_beg, global_end, heap_beg, heap_end, stack_beg, stack_end, i}
```

Memory assumptions:

$$\begin{aligned} & global\_beg \leq global\_end \wedge global\_end < heap\_beg \wedge \\ & heap\_beg \leq heap\_end \wedge heap\_end < stack\_end \wedge \\ & stack\_end \leq stack\_beg \wedge global\_beg = global\_end \wedge \end{aligned}$$
$$heap\_beg = heap\_end \wedge i = stack\_beg - 4 \wedge stack\_end = stack\_beg - 4$$

VC:  $read(mem@i) == 0$

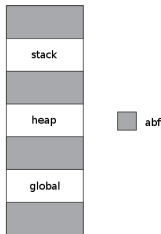
- ▶ “is reading value 0 at memory position  $i$  possible”?
- ▶ UNSAT if assertion holds (on path)



# (Simple) Assignment Check

- ▶ validity of address (*addr*) a value is assigned to
- ▶ introduce *abf* outside *any* valid memory:

*abf* > *stack\_beg* ∨  
*abf* > *global\_end* ∧  
*abf* < *heap\_beg* ∨  
*abf* > *heap\_end* ∧  
*abf* < *stack\_end* ∨  
*abf* < *global\_beg*



- ▶ VC: *abf* == *addr*
  - ▶ “can *addr* be equal to an address outside valid memory?”
  - ▶ SAT if *addr* is invalid